



Multidimensional Poverty Measurement and Analysis

Sabina Alkire, James Foster, Suman Seth, Maria Emma Santos, José Manuel Roche and Paola Ballon

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MULTIDIMENSIONAL POVERTY MEASUREMENT AND ANALYSIS

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Comprehensive survey of methods used for measuring multidimensional poverty

Illustrates state-of-the-art of quantitative techniques used in multidimensional poverty studies

A unique guide to viewing poverty through a multidimensional lens

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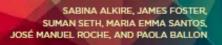
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Background

Motivation:

- Normative: Capability Sen, A. K. (1992). *Inequality Re-examined*. Oxford: Oxford University Press.
- Empirical: Mis-match
- Stewart, F., Saith, R., and Harriss-White, B. (2007). *Defining Poverty in Developing Countries*. Basingstoke: Palgrave Macmillan.
- Bourguignon, F., Bénassy-Quéré, A., Dercon, S., Estache, A., Gunning, J.W., Kanbur, R., Klasen, S., Maxwell, S., Platteau, J-P., and A. Spadaro (2010) 'Millennium Development Goals: An Assessment', in R. Kanbur and M. Spencer (eds.), *Equity and Growth in a Globalizing World*. World Bank, ch. 2.
- **Policy:** Atkinson, A. B. (2003). 'Multidimensional Deprivation: Contrasting Social Welfare and Counting Approaches', *Journal of Economic Inequality*, 1(1):51-65.



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Methods:

- Dashboard: Ravallion, M. (2011b). 'On Multidimensional Indices of Poverty', *Journal of Economic Inequality*, 9(2): 235–48.
- **Composite:** Nardo, M., Saisana, M., Saltelli, A., Tarantola, S., Hoffman, A., and Giovannini, E. (2008). *Handbook on Constructing Composite Indicators: Methodology and User Guide*. Ispra, Italy: OECD.



Methods:

- **Dominance:** Duclos, J. Y., Sahn, D. E., and Younger, S. D. (2006a). 'Robust Multidimensional Poverty Comparisons', *The Economic Journal*, 116(514): 943–68.
- Statistical: Asselin, L. M. (2009). *Analysis of Multidimensional Poverty: Theory and Case Studies*. Dordrecht: Springer.
- Fuzzy: Lemmi, A. and Betti, G. (2006). Fuzzy Set Approach to Multidimensional Poverty Measurement. New York: Springer.
- Axiomatic: Bourguignon, F. and Chakravarty, S. R. (2003). 'The Measurement of Multidimensional Poverty', *Journal of Economic Inequality*, 1(1): 25–49.
- **Counting:** Nolan, B. and Whelan, C. (2011). *Poverty and Deprivation in Europe*. Oxford: Oxford University Press.



Moving Forward: Axiomatic & Counting

- Identification: Sen, A. K. (1976). 'Poverty: An Ordinal Approach to Measurement', *Econometrica*, 44(2): 219–31.
- **Decomposability:** Foster, J. E., Greer, J., and Thorbecke, E. (1984). 'A Class of Decomposable Poverty Measures', *Econometrica*, 52(3): 761–6.
- Functionings & Counting: Brandolini, A., D'Alessio, G., 1998. Measuring Well-being in the Functioning Space. Mimeo. Rome. Banco d'Italia Research Department.





The Alkire-Foster Methodology

Multidimensional Data

Matrix of well-being scores for n persons in d dimensions

Dimensions

$$X = \begin{bmatrix} 13.1 & 14 & 4 & 1 \\ 15.2 & 7 & 5 & 0 \\ 12.5 & 10 & 1 & 0 \\ 20 & 11 & 3 & 1 \end{bmatrix}$$
 Persons
$$z = (13 \quad 12 \quad 3 \quad 1)$$
 Cutoffs



Multidimensional Data

Replace entries: 1 if deprived, 0 if not deprived

Dimensions

$$X = \begin{bmatrix} 13.1 & 14 & 4 & 1 \\ 15.2 & 7 & 5 & 0 \\ 12.5 & 10 & 1 & 0 \\ 20 & 11 & 3 & 1 \end{bmatrix}$$
 Persons
$$z = (13 \quad 12 \quad 3 \quad 1)$$
 Cutoffs

These entries fall below cutoffs



Deprivation Matrix

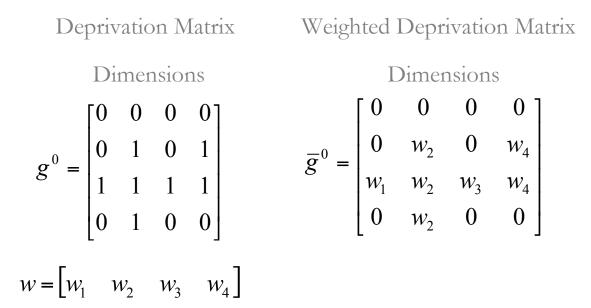
Replace entries: 1 if deprived, 0 if not deprived

Dimensions

$$g^{0} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$
 Persons



Identification – Weights







Identification – Counting Deprivations Assuming equal weights and $\sum_{j=1}^{d} w_j = d$

		mer			С			
$\overline{g}^0 =$	0 0 1	0	0	0]	0			
	0	1	0	1	2	Domona		
	1	1	1	1	4	Persons		
	0		0					



Identification

Q/ Who is poor?

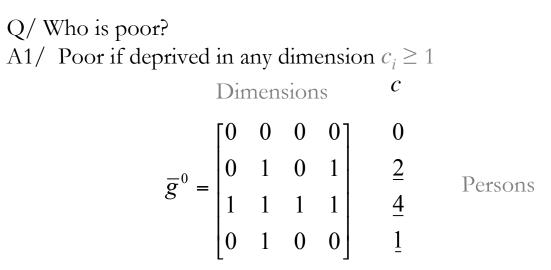
	Din	nen	sion	lS	С			
$\overline{g}^0 =$	[0	0	0	0]	0			
	$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	1	0	1	2	Dorradia		
	1	1	1	1	4	Persons		
	0	1	0	0	1			



Identification – Union Approach



Identification – Union Approach



Observations

Union approach often predicts very high numbers.

Charavarty et al '98, Tsui '02, Bourguignon & Chakravarty 2003 etc use the union approach



Identification – Intersection Approach



Identification – Intersection Approach

Q/ Who is poor? A2/ Poor if deprived in all dimensions $c_i = d$ Dimensions c $\overline{g}^0 = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 \\ 2 \\ 4 \\ 1 \end{bmatrix}$ Persons

Observations

Demanding requirement (especially if d large) Often identifies a very narrow slice of population Atkinson 2003 first to apply these terms.



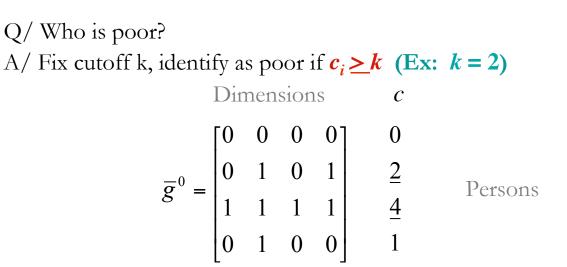
Identification – Dual Cutoff Approach

Q/ Who is poor? A/ Fix cutoff *k*, identify as poor if $c_i \ge k$

	Dir	nen	sion	IS	С	
$\overline{g}^0 =$	[0	0	0	0]	0	
	0	1	0	1	2	D
	0 0 1 0	1	1	1	4	Persons
	0	1	0	0	1	



Identification – Dual Cutoff Approach





Identification – Empirical Example

	<i>k</i> =	Н
	Union 1	91.2%
ſ [2	75.5%
	3	54.4%
Γ	4	33.3%
	5	16.5%
	6	6.3%
	7	1.5%
Γ	8	0.2%
	9	0.0%
	Inters. 10	0.0%

Poverty in India for 10 dimensions

91% of population wouldbe targeted using union0% using intersection

We need something in the middle (*Alkire and Seth 2009*)

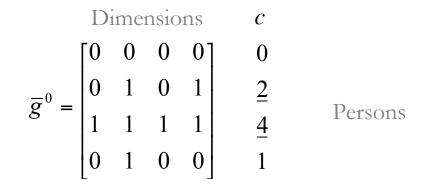




Aggregation

k = 2

Censor data of non-poor





Aggregation

k = 2

Censored weighted deprivation matrix and censored deprivation score

	Di	mei	nsio	ns	c(k)	
$\overline{g}^{0}(k) =$	[0	0	0	0]	0	Persons
	0	1	0	1	<u>2</u>	
	1	1	1	1	<u>4</u>	
	0	0	0	0	0	



Aggregation – Headcount Ratio

k = 2

Censored weighted deprivation matrix

$$\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
Persons

Two poor persons out of four: H = 1/2



Critique

Suppose the number of deprivations rises for person 2

	D	c(2)			
	[0	0	0	[0	0
$\overline{g}^{0}(2) =$	1	1	0	1	<u>3</u>
g(2) =	1	1	1	1	<u>4</u>
	0	0	0	0	0



Critique

Suppose the number of deprivations rises for person 2

	Di	<i>c</i> (2)			
	[0	0	0	[0	0
$\overline{g}^{0}(2) =$	1	1	0	1	<u>3</u>
g(2) =	1	1	1	1	<u>4</u>
	0	0	0	0	0

Two poor persons out of four: H = ½ No change! Violates 'dimensional monotonicity'



Aggregation

Return to the original censored weighted deprivation matrix

	Di	men	isio	ns	c(2)	
	[0	0	0	[0	0	
$\overline{g}^{0}(2) =$	0	1	0	1	<u>2</u>	Persons
	1	1	1	1	<u>4</u>	
	0	0	0	0	0	



Need to augment information Deprivation shares among poor $\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$



Aggregation - Intensity

Need to augment information Deprivation shares among poor $\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

A = average deprivation share among poor = 3/4



Aggregation - Intensity

Aggregation: Adjusted Headcount Ratio Adjusted Headcount Ratio = M_0 = HA

Dimensions
$$c(k) \quad c(k)/d$$

$$\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{array}{c} 0 & & \\ 2 & 2/4 \\ 4 & 4/4 \\ 0 & \end{array}$$
Persons

 $M_0 = HA = (1/2)^*(3/4) = 0.375$



Aggregation: Adjusted Headcount Ratio Adjusted Headcount Ratio = $M_0 = HA = \mu(\overline{g}^0(k))$

Dimensions
$$c(k) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 2 & 2/4 \\ 0 & 4/4 \end{bmatrix}$$

 $M_0 = HA = (1/2)^*(3/4) = 0.375$ $M_0 = \mu(\overline{g}^0(k)) = 6/16 = 0.375$



Aggregation: Adjusted Headcount Ratio

Suppose the number of deprivations rises for person 2

Dimensions
$$c(k) \ c(k)/d$$

$$\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{array}{c} 0 \\ \frac{3}{2} & 3/4 \\ \frac{4}{4} & 4/4 \end{array} \text{ Persons}$$



Aggregation: Adjusted Headcount Ratio

Suppose the number of deprivations rises for person 2

Dimensions
$$c(k) \ c(k)/d$$

$$\overline{g}^{0}(2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & \frac{3}{4} & \frac{3}{4} & 0 \\ 0 & \frac{4}{4} & \frac{4}{4} & 0 \end{bmatrix}$$
Persons

A = average deprivation share among poor = 7/8 M_0 changes! $M_0 = 7/16 = 0.4375$

Satisfies dimensional monotonicity



Methodology: Adjusted Headcount Ratio

Interpretation: conveys information on deprivations

Applicability: valid for ordinal data

Simplicity: easy to compute

Useful properties

- Subgroup decomposition
- Dimensional breakdown

Expandable: If variables are all cardinal can go further



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Countries

This methodology can be used to design robust official statistics

Official multidimensional poverty statistics are used in Mexico, Colombia, Bhutan, Chile and others.

This book can be useful for technical advisors in countries that are exploring or actively designing multidimensional poverty measures

The <u>MPPN</u> (Multidimensional Poverty Peer Network) is a network of some 40 countries with such an interest.

It can also be used for designing other policy-relevant indices

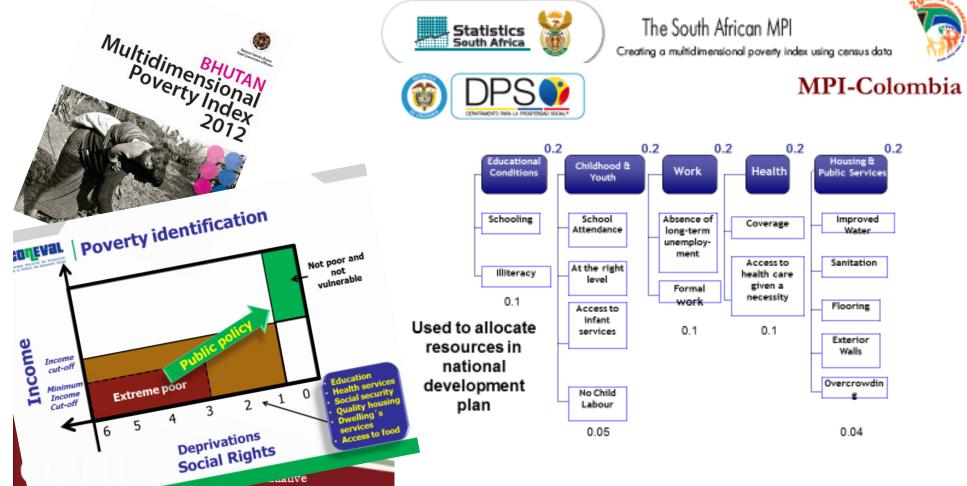
Examples: Well-being, Child Poverty, Empowerment (WEAI)



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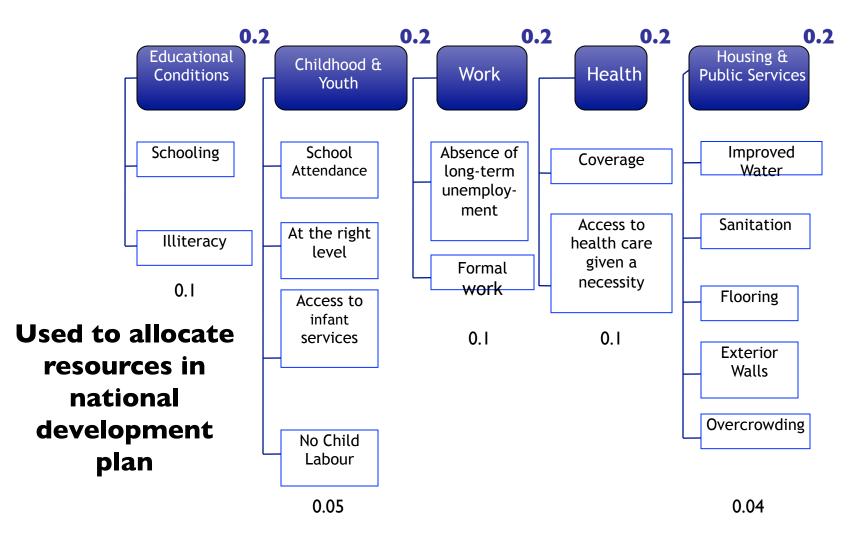
National MPIs

- Reflect National Priorities
- Vital for policy
- Measure to Manage ~ Target, Coordinate, M&E





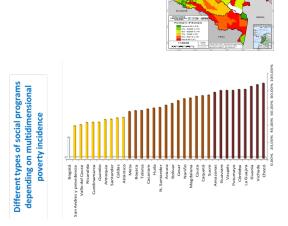






- 1. Reflects the objectives of social policy
- 2. Coordinates public policy sectors
- 3. Monitors public policy
- 4. Informs Decision-making:
 - 1. Geographic targeting
 - 2. Programme composition
 - 3. Graduation from CCTs





International Agencies & Civil Society

Use for Programme Quality (inward looking)

Diagnostic and prioritization

Baseline and M&E tool

Applied to distinct domains (poverty, empowerment, child rights, etc)

Understanding underlying multidimensional processes

Multidimensional measures force institutions to break silos, and to discuss interaction between dimensions!





Save the Children

World Vision®

Oxfam

unicef 🥴

International Agencies & Civil Society

Use for Policy & Research or Advocacy (outward looking)

Accountability tool to hold governments to account

Monitoring multidimensional outcomes (Global MPI, UNICEF MODA, MPI & Post2015)

Policy analysis for evidence based advocacy



Teaching

Masters/PhD level courses

- ✓ Module on poverty measurement
- ✓ Comprehensive overview for teachers
- ✓ Unified notation and framework

From book website: http://multidimensionalpoverty.org/

- ✓ Online chapters
- ✓ Video presentations
- ✓ PowerPoints
- ✓ Paper exercises
- \checkmark Stata do files for statistical exercises



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Chapter 3 – Overview of Methods for Multidimensional Poverty Assessment

Overview:

This chapter presents a constructive survey of the major existing methods for measuring multidimensional poverty. Many measures were motivated by the basic needs approach, the capability approach, and the social inclusion approach among others. This chapter reviews Dashboards, the composite indices approach, Venn diagrams, the dominance approach, statistical approaches, fuzzy sets, and the axiomatic approach. The first two methods (dashboard and composite indices) methods that are implemented using aggregate data from different sources ignoring the joint distribution of deprivations. The other methods reflect the joint distribution and are implemented using data in which information on each dimension is available for each unit of analysis. After outlininge each method, we provide a critical evaluation by discussing its advantages and disadvantages.

Read Full Chapter

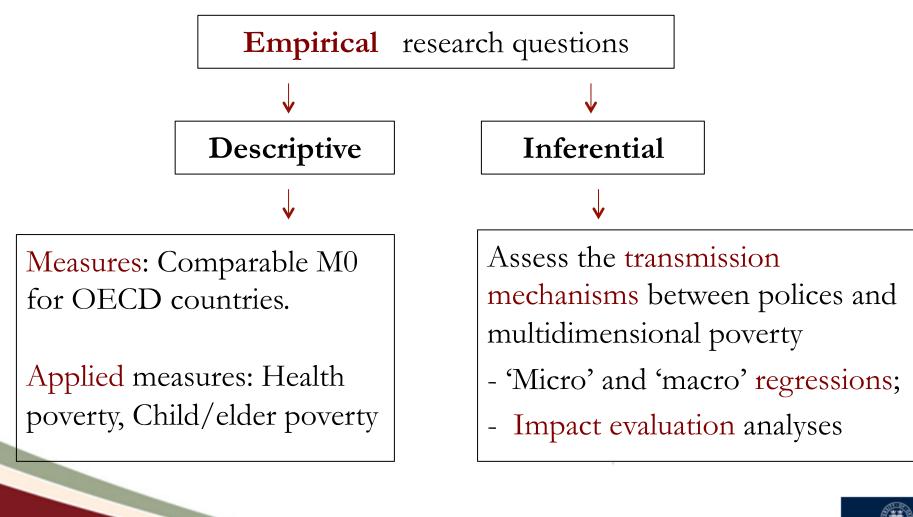
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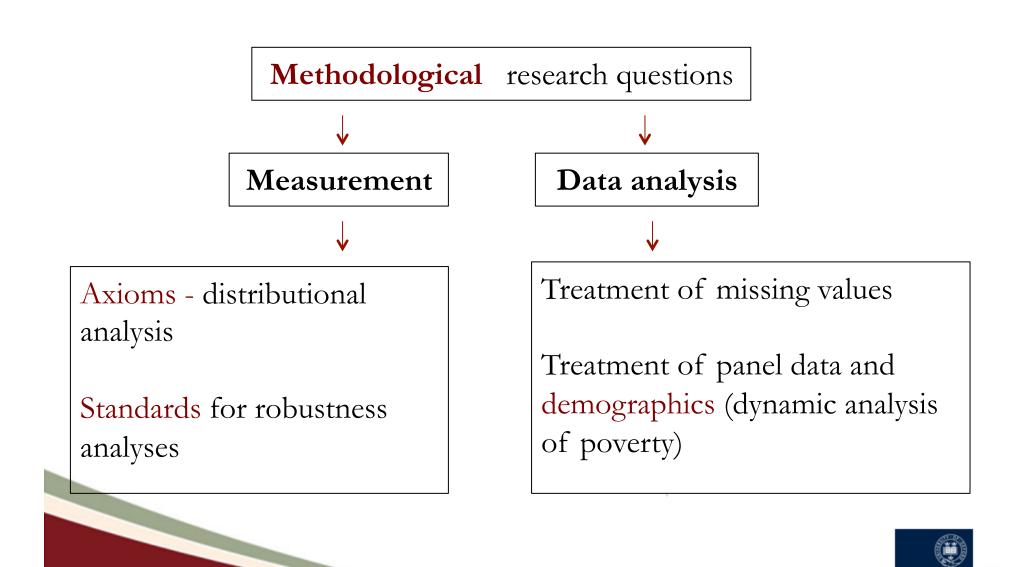
Researchers







Researchers



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